

Course Code: 3MSCM2
 Course: Integral Transform-I
 Credit: 4
 Last Submission Date: April 30 (for January Session)
 October 31, (for July session)

Max. Marks:-70
 Min. Marks:-25

Note:-attempt all questions.

Que.1 State & Prove Initial & Final value theorem.

Que.2 Solve the Following by replace transform

1. $e^{-2t} (3\cos 6t - 5\sin 6t)$
2. $e^t \sin^2 t$
3. $t^2 \cos at$
4. $\frac{\sin at}{t^2}$
5. $\int_0^\infty \frac{\sin t}{t} dt = \frac{\pi}{2}$

Que.3 Solve $\frac{d^4 y}{dx^4} + m^4 y = 0$

Que.4 Solve $\frac{d^2 y}{dx^2} + a^2 y = \sec(ax)$

Que.5 The initial temperature of a slab of homogenous material bounded by the planes $x = 0$ and $x = L$ is to find the temperature in this solid after the face $x = 0$ is insulated and the temperature of face $x = L$ is reduced to zero.

Que.6 A string is stretched between two fixed points $(0,0)$ and $(c,0)$. If it is displaced into the curve $y = b \sin\left(\frac{\pi x}{c}\right)$ and released from rest in that position at time $t = 0$, find its displacement at any time $t > 0$ and any point $0 < x < c$.

Que.7 Find the Fourier transform of

$$f(x) = \begin{cases} 1 - x^2, & |x| \leq 1 \\ 0, & |x| > 1 \end{cases}$$

Que.8 Find the sine and cosine transform of

$$\frac{e^{ax} + e^{-ax}}{e^{\pi x} - e^{-\pi x}}$$

Que.9 Find the finite Fourier sine and cosine transform of $f(x) = x$

Que.10 Find the finite cosine transform of

$$\left(1 - \frac{x}{\pi}\right)^2$$