w.e.f: July 2018

SYLLABUS

MASTER OF SCIENCE (M.Sc.) -MATHS

2018-19

DR. C.V. RAMAN UNIVERSITY

KARGI ROAD, KOTA, BILASPUR, CHATTISGARH

PHONE : 07753-253737, 8827920016, 8827920019 FAX : 07753-253728

E-mail: iode@cvru.ac.in Website: www.cvru.ac.in

w.e.f: July 2018

DR. C.V.RAMAN UNIVERSITY

KARGI ROAD, KOTA, BILASPUR (C.G.)

MASTER OF SCIENCE (MATHEMATICS)

Duration - 24 Months (2 Years) Eligibility - Graduation with Maths Subject

SCHEME OF EXAMINATION

Course Code	Nature of the Course	Name of Course	Credit			Total Credits	Total Marks	Theory		Practical Marks		Assignment	
			L	P	T			Max	Min	Max	Min	Max	Min
First Semester													
4010111401	Core	Advanced Abstract Algebra-I	3	-	1	4	100	70	28	-	-	30	15
4010111402	Core	Real Analysis-I	3	-	1	4	100	70	28	-	-	30	15
4010111403	Core	Topology-I	3	-	1	4	100	70	28	-	-	30	15
4010111404	Core	Complex Analysis-I	3	-	1	4	100	70	28	-	-	30	15
4010111405	Core	Differential Equation-I	3	-	1	4	100	70	28	-	-	30	15
Total			**15**	**-**	**05**	**20**	**500**	**350**	**140**	**0**	**0**	**150**	**75**
Second Semester													
4010211401	Core	Advanced Abstract Algebra-II	3	-	1	4	100	70	28	-	-	30	15
4010211402	Core	Real Analysis-II	3	-	1	4	100	70	28	-	-	30	15
4010211403	Core	Topology-II	3	-	1	4	100	70	28	-	-	30	15
4010211404	Core	Complex Analysis-II	3	-	1	4	100	70	28	-	-	30	15
4010211405	Core	Differential Equation-II	3	-	1	4	100	70	28			30	15
Total			**15**	**-**	**05**	**20**	**500**	**350**	**140**	**0**	**0**	**150**	**75**
Third Semester													
4010311401	Core	Functional Analysis-I	3	-	1	4	100	70	28	-	-	30	15
4010311402	Core	Integral Transform-I	3	-	1	4	100	70	28	-	-	30	15
4010311403	Core	Partial Differential Equation	3	-	1	4	100	70	28	-	-	30	15
	Discipline Specific Elective	Elective-I	3	-	1	4	100	70	28	-	-	30	15
	Discipline Specific Elective	Elective-II	3	-	1	4	100	70	28	-	-	30	15
Total			**15**	**-**	**05**	**20**	**500**	**350**	**140**	**0**	**0**	**150**	**75**
Fourth Semester													
4010411401	Core	Functional Analysis-II	3	-	1	4	100	70	28	-	-	30	15
4010411402	Core	Integral Transform-II	3	-	1	4	100	70	28	-	-	30	15
	Discipline Specific Elective	Elective-III	3	-	1	4	100	70	28	-	-	30	15
	Discipline Specific Elective	Elective-IV	3	-	1	4	100	70	28	-	-	30	15
4010431401	Research Component	Project Work	-	4	-	4	100	-	-	100	50	-	-
		Total	**12**	**4**	**04**	**20**	**500**	**280**	**112**	**100**	**50**	**120**	**60**

Evaluation Scheme

- The minimum Marks required to pass any theory paper in a Semester shall be 40 %.
- The minimum Marks required to pass in Project works/ Practical/ Assignments/Dissertation shall be 50%.

LIST OF ELECTIVES

***Note** - Students need to select two paper from each elective for third & fourth semester.

Elective Paper Third Semester **Elective Paper Fourth Semester**

Codes	Nature of the Course	List of Electives	Codes	Nature of the Course	List of Electives
Elective -I			**Elective -III**		
4010341402	Discipline Specific	Advanced Discrete Mathematics	4010441411	Discipline Specific	Metric Spaces and Fixed Point Theory
4010341406	Discipline Specific	Numerical Analysis	4010441412	Discipline Specific	Measure and Integration Theory
4010341407	Discipline Specific	Mathematical Statistics	4010441413	Discipline Specific	Object Oriented Programming
Elective -II			**Elective -IV**		
4010341408	Discipline Specific	Special Function	4010441405	Discipline Specific	Operations Research
4010341409	Discipline Specific	Differential Geometry	4010441414	Discipline Specific	Fuzzy Set Theory
4010341410	Discipline Specific	Number Theory	4010441415	Discipline Specific	Advanced Graph Theory

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Kargi Road, Kota, Bilaspur (C.G.)

SEMESTER- 1st **Subject Code: 4010111401**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: ADVANCED ABSTRACT ALGEBRA-I **Theory Min. Marks: 28**

Objectives:

- This course aims to provide a first approach to the subject of algebra, which is one of the basic pillars of modern mathematics.
- The focus of the course will be the study of certain structures called groups, rings, fields and some related structures.
- In particular to study in details the Sylow theorems and polynomials rings.
- This course helps to gain skill in problem solving and critical thinking.
- Abstract algebra is a classical field that is associated with the study of polynomials in several variables.

Unit-1

Class equation of finite group, Center for group of prime-power order, Cauchy's theorem for finite groups, Sylow's First, Second and Third Theorems, P-Sylow subgroup, Double Coset, Conjugate subgroup.

Unit-2

Normal and subnormal series of group, Composition series of group, Jordan- Holder theorem, Solvable and Nilpotent groups.

Unit-3

Polynomials Ring R[x], Primitive polynomial, Irreducibilty Criterion, Polynomial rings over commutative rings, Unique Factorization Domain.

Unit-4

Field & subfield definition & examples, Extension fields, Algebraic & Transcendental extensions , Separable and Inseparable extensions, Normal extension.

Unit-5

Perfect fields, Finite fields, Primitive elements, Algebraically closed fields, Automorphisms of extensions, Galois extensions, Fundamental theorem of Galois theory.

Outcomes:

- The student will be able to define the concepts of group, ring, field, and will be able to readily give examples of each of these kinds of algebraic structures.
- The student will be able to define the concepts of coset and normal subgroup and to prove elementary propositions involving these concepts.
- The student will be able to define the concept of subgroup and will be able to determine (prove or disprove), in specific examples, whether a given subset of a group is a subgroup of the group.
- The student will be able to define and work with the concepts of homomorphism and isomorphism.
- The student will be able to apply the basic concepts of field theory, including field extensions and finite fields.

Text book:

- S.K. Jain, P.B. Bhattacharya and S.R. Nagpaul, Basic Abstract Algebra, Cambridge University Press (1997)
- H.K Pathak, Advanced Abstract Algebra, Sahitya Prakashan Merath.

References Book:

- J.N. Sharma A.R.Vashishtha, Abstract Algebra, Krishna Prakashan Media (P) Ltd. Meerut Delhi.
- Shanti Narayan, Modern Abstract Algebra, S.Chand & Co. New Delhi.
- R.S.Verma, Algebra, Pathshala Pvt. Ltd. Allahabad.

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SEMESTER- 1st | **Subject Code: 4010111402**
Course: M.Sc. Mathematics | **Theory Max. Marks: 70**
SUBJECT: REAL ANALYSIS-I | **Theory Min. Marks: 28**

Objectives:

- The goal of this course is for students to gain proficiency in convergence, test of sequences and series of real numbers.
- To familiarize the student with open set and closed set of real numbers.
- To make the student acquire sound knowledge of techniques in solving differential calculus.

Unit-1

Sequences & subsequences, Convergent sequence, divergent sequence and some theorems, Real Valued function & Theorems, Cesaros's Theorem, Nested Interval theorem, Limit superior and Limit Inferior.

Unit-2

Series of Non-negative terms, comparison test, cauchy's condensation test, comparison of ratios, Logarithmic test, D'morgan and bertrand's test.

Unit-3

General Principal of convergence, pringsheims Method, Merten's Theorem, Abel's Theorem, Euler's constant Theorem.

Unit-4

Neighbourhoods, open set and closed set & properties, Bolzano-weierstranss Theorem, Baire category theorem for R, covering Theorem.

Unit-5

Limit and continuity Theorems on continuity, Bolzano's theorem on continuity, continuity of inverse function, Geometrical meaning of a derivative, chain Rule of Derivative, Darboux Theorem and cauchy's mean value Theorems.

Outcomes:

- Fluency in convergence test using standard methods, including the ability to find an appropriate test for a given sequence or series.
- Understanding ideas and concept of differential calculus and facility in solving standard examples.
- Understanding the ideas of open and closed sets and facility in solving standard examples.

Text book:

- H.K Pathak, Real Analysis, Siksha Sahitya Prakashan Meerut.
- J.N.Sharam & R. Vasisth, Real Analysis, Krishna Publication, Pvt. Ltd.

References Book:

- Valter Royden, Principle of Mathematical Analysis, Tata McGraw Hill.
- P.K. Jain & N.K.Ahamed, Metric Spaces, Narosa Publishing House New Delhi 1996.
- P.K.Jain & S.K. Kaushik, An Introduction to real analysis, S.Chand & Co. New Delhi.

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SEMESTER- 1st | **Subject Code: 4010111403**
Course: M.Sc. Mathematics | **Theory Max. Marks: 70**
SUBJECT: TOPOLOGY-I | **Theory Min. Marks: 28**

Objectives: The aim of this course is to provide students

- An introduction to theory of metric and topological spaces with emphasis on those topics that are important to higher mathematics.
- Basic notions of metric and topological spaces.
- Information about the properties of continuous mappings and convergence in topological spaces.
- The broader information of some selected types of topological spaces (compact, product, connected spaces) and countability, separation axioms including some basic theorems on topological spaces.
- Information about product invariance of certain separation and countability axioms.

Unit-1

Definition and examples of topological space, Opensets, Closed sets , Closure , Dense subsets.

Unit-2

Neighborhoods , Interiors ,exteriors and boundry .Accumulation point and derived sets ,bases and sub-bases, subspaces and relative topology .

Unit-3

Continuous Maps, Continuous Maps into R, open and closed maps, Homeomorphism, Finite product spaces, projection maps.

Unit-4

Connected space and disconnected spaces, separated sets, component, locally connected space, Path connectedness, separation axioms : T0, T1 and T2 Spaces.

Unit-5

Introduction of compactness, compact subspace, Finite intersection property, Bolzano-weierstrass property, countable, sequential and local compactness.

Outcomes: Upon successful completion of the program the students will be aware of:-

- The definitions of standard terms in topology.
- How to read and write proofs in topology with a variety of examples and counter examples.
- Some important concepts like continuity, compactness, connectedness, projection mapping etc
- Countability, separation axioms and convergence in topological spaces.
- Using new ideas in mathematics and also help them in communicating the subject with other subjects.

Text book:

- J.N. Sharma, Topology, Krishan Prakashan Media (P) Ltd. Meerut Delhi.
- J.M. Munkers, Topology, Publication Tata McGraw Hill.
- H.K.Pathak, Topology, Shisksha Sahitya Prakashan Meerut.

References Book:

- G.F. Simmons, Introduction to topology and modern analysis, Tata McGraw Hills.
- K.D.Joshi, Introduction to General Topology, Wiley Eastern.

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SEMESTER- 1st **Subject Code: 4010111404**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: COMPLEX ANALYSIS-I **Theory Min. Marks: 28**

Objectives:

- To tell more about complex numbers and complex valued function to the students.
- To introduce the concept of conformal mapping and Bilinear transformation of different kind.
- To introduce the concept of complex integration on simply connected region and multiple connected region.
- To introduce three main and important theorem of Complex Analysis namely Liouvilles theorem, Morera's theorem and Cauchy's integral formula.
- To introduce Taylor's series and Laurent's series to the students.

Unit-I

Complex Number, Analytic Functions, Cauchy – Riemann Equations, Harmonic Functions, Conjugate functions.

Unit-II

Conformal mappings, Bi-linear transformations, Geometrical interpretations of the transformations $\omega = z+\alpha$, $\omega = \beta z$, $\omega = \gamma z$. Bi-linear transformation of a circle.

Unit-III

Complex integration, complex integrals as sum of two real line integrals, Cauchy's Theorem, Extension of cauchy's Theorem to multi – connected region Cauchy.

Unit-IV

Cauchy integral formula, Extension of cauchy's integral formula to multiconnected regions, Liouville's Theorem, Morea's theorem.

Unit-V

Taylor's Theorem, Laurent's Theorem with examples.

Outcomes:-

- Understanding about complex number and complex valued function will enable them to deal with function of multi variable.
- Students will able to transform the region /object of one plane onto another plane easily.
- Cauchy theorem will help them to find the integration of function on the region where function is analytic and where it is not Analytic.
- Cauchy integral formula with help students to find the value of function at inside point of the region.
- Students will able to expand function in series of positive and negative power of variable in a given region.

Text book:

- Dr. H.K. Pathak, Complex Analysis, Shiksha Sahitya Prakashsn Meerut.
- J.N. Sharma, Complex Functions, Krishan Prakashan Media (P) Ltd. Meerut Delhi.

References Book:

- V.S.Tyagi, Functions of a complex variable, Kedarnath Ramanath Delhi.
- S. Ponnusony, Foundation of Complex analysis, Narosa Publishing House.
- John & Mathews Russell Wottowell, Complex analysis for Mathematics & Engineering.

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SEMESTER- 1st **Subject Code: 4010111405**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: DIFFERENTIAL EQUATION-I **Theory Min. Marks: 28**

Objective

- This course helps the students to study elementary concepts.
- To introduce the concept of simultaneous differential equations.
- Understanding the concept of integration in series.
- To understand the Existence and Uniqueness theorem.

Unit-1

Elementary Concepts: Linear equations of second order, Transformation of the equation to the normal form, Transformation of the equation by changing the independent variable, Method of variation of parameters.

Unit-2

Ordinary simultaneous differential equations, Differential equations in different form, Total differential equation.

Unit-3

Integration in series : Roots of indicial equation equal, Roots of indicial equation unequal and differing by a quantity not an integer, Roots of indicial equation equal differing by an integer making coefficient of y-infinity.

Unit-4

Roots of indicial equation differing by an integer ; making a coefficient of y indeterminate, Some cases where the method fails, The particular integral, Method of differentiation.

Unit-5

Picard's iteration method, The Lipschitz condition, Existence theorem, Uniqueness theorem, Existence and Uniqueness theorem (The general case).

Text book:

- Sharma-Gupta, Differential Equation, Krishan Prakashan Media (P) Ltd. Meerut Delhi.
- H.K Pathak, Differential Equation, Shiksha Sahitya Prakashan Meerut.

Refferences Book:

- Ravi P.Agrawal and Ramesh C.Gupta, "Essentials of Ordinary Differential Equations" , Mc Graw-Hill Book Company,1993.
- Elsgolts, " Differential equation and the calculus of variations" ,MIR publications,1980.

Outcomes:

- The student will be able to define the elementary concept of differential equations.
- The student will be able to define and work with the concept of simultaneous differential equations.
- The student will be able to define and work with the concept of integration in series.
- The student will be able to apply the iteration method.

Text book:

- S.K. Jain, P.B. Bhattacharya and S.R. Nagpaul, Basic Abstract Algebra, Cambridge University Press (1997)
- H.K Pathak, Advanced Abstract Algebra, Sahitya Prakashan Merath.

References Book:

- J.N. Sharma A.R.Vasist, Abstract Algebra, Krishan Prakashan Media (P) Ltd. Meerut Delhi.
- Shanti Narayan, Modern Abstract Algebra, S.Chand & Co. New Delhi.
- R.S.Verma, Algebra, Pathshala Pvt. Ltd. Allahabad.

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SEMESTER- 2nd **Subject Code: 4010211401**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: ADVANCED ABSTRACT ALGEBRA-II **Theory Min. Marks: 28**

Objectives:

- The focus of the course will be the study of modules over a ring.
- In particular to study in details the Noetherian and Artinian modules and rings.
- This course helps to study the Linear transformations, Algebra of Linear transformations & Linear operators.
- In particular to study in details the Nilpotent transformations, Jordan blocks & forms.
- This course helps to study the fundamental structure theorem of modules over PID and also helps to gain knowledge about its application to finitely generated abelian group.

Unit-1

Modules, Quotient modules, Module homomorphism, Module isomorphism, Finitely generated module.

Unit-2

Cyclic modules, Simple modules, Semi-simple modules, Schur's lemma, Noetherian & Artinian modules and rings, Hilbert Basis theorem, Wedderburn Artin theorem, Uniform modules, Primary modules.

Unit-3

Linear transformations, Algebra of linear transformation, Algebra of linear operators, Range and Null space of linear transformations, Characteristic roots, Matrices and linear transformations.

Unit-4

Similarity of linear transformations, Invariant subspaces, Nilpotent transformations, Index of nilpotency, Invariants of a nilpotent transformation, Jordan blocks and Jordan forms, Primary decomposition theorem.

Unit-5

Smith normal form over a principal ideal domain and rank, Fundamental structure theorem for finitely generated modules over a principle ideal domain and its applications to finitely generated abelian groups.

Outcomes:

- The student will be able to define the concepts of module over a ring and will be able to readily give examples of this kinds of algebraic structures.
- The student will be able to define and work with the concepts of Noetherian and Artinian modules and rings.
- The student will be able to define the concept of Linear transformations, Algebra of Linear transformations & Linear operators, Nilpotent transformations, Jordan blocks & forms.
- The student will be able to give detail proof and work with the concepts of Schur's Lemma.
- The student will be able to apply the basic concepts of modules, including uniform and primary modules.

Text book:

- S.K. Jain, P.B. Bhattacharya and S.R. Nagpaul, Basic Abstract Algebra, Cambridge University Press (1997)
- H.K Pathak, Advanced Abstract Algebra, Sahitya Prakashan Merath.

References Book:

- J.N. Sharma A.R.Vashishtha, Abstract Algebra, Krishna Prakashan Media (P) Ltd. Meerut Delhi.
- Shanti Narayan, Modern Abstract Algebra, S.Chand & Co. New Delhi.
- R.S.Verma, Algebra, Pathshala Pvt. Ltd. Allahabad.

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SEMESTER- 2nd
Course: M.Sc. Mathematics
SUBJECT: REAL ANALYSIS-II

Subject Code: 4010211402
Theory Max. Marks: 70
Theory Min. Marks: 28

Objectives:

- To make familiarize the student with Riemann-Stieltjes integral and their application.
- To make the student acquire sound knowledge of techniques in solving problems on function of several variable and Jacobian .

Unit-1

Definition of Riemann-Stieltses Integral & theorems, The Rs-Integral as limit of sums, Some classes of Rs-Integrable function, Algebra of Rs-Integrable function, The Interval of integration, The Rs-Integrability of composite function.

Unit-2

Relation between R- Integral & Rs-Integral, Integration of vector valued function, some more Theorems on integration.

Unit-3

Continuity of function of two variables, Partial Derivatives, Differentiability of two variables, Differentiability of composite function.

Unit-4

Differentiation, Differentiation of vector-valued function, Differentiation in Rn, The implicit function Theorem.

Unit-5

Definition of Jacobians', Case of function of function, Jacobian of implicit functions, Necessary and Sufficient condition for a Jacobian to Vanish Identically.

Outcomes:

- Understanding ideas and concept of Riemann – Stieltjes integral and facility in solving standard examples.
- Fluency in solving standard methods, including the ability to find an appropriate method for a given function of several variables.
- Understanding the ideas of Jacobian and facility in solving standard examples.

Text book:

- H.K. Pathak, Real Analysis, Siksha Sahitya Prakashan Meerut.
- J.N. Sharma & R. Vasisth, Real Analysis, Krishna Publication, Pvt. Ltd.

References Book:

- Walter Royden, Principle of Mathematical Analysis, Tata McGraw Hill.
- P.K. Jain & N.K.Ahamed, Metric Spaces, Narosa Publishing House New Delhi 1996.
- P.K.Jain & S.K. Kaushik, An Introduction to real analysis, S.Chand & Co. New Delhi.

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SEMESTER- 2nd
Course: M.Sc. Mathematics
SUBJECT: TOPOLOGY-II

Subject Code: 4010211403
Theory Max. Marks: 70
Theory Min. Marks: 28

Objectives: The aim of this course is to provide students

- An introduction to theory of metric and topological spaces with emphasis on those topics that are important to higher mathematics.
- Basic notions of metric and topological spaces.
- Information about the properties of continuous mappings and convergence in topological spaces.
- The broader information of some selected types of topological spaces (compact, product, connected spaces) and countability, separation axioms including some basic theorems on topological spaces.
- Information about product invariance of certain separation and countability axioms.

Unit-1

Separation Axioms: Regular and T3 spaces, normal and T4 spaces, Urysohn's Lemma, Tietze's, Extension theorem, completely regular and Tychonoff spaces, completely normal and T5 spaces.

Unit-2

Countablility Axioms: First and second axioms of countablility, Lindelof spaces , Separable spaces , Coutably compact spaces, Limit point compact spaces.

Unit-3

Convergence in Topology: Sequences and subsequences, convergence in topology, sequential compactness, local compactness, one point compactification, Stone-Cech compactification.

Unit-4

Metric Spaces and Metrizability: Separation and countability axioms in metric spaces, convergence in metric spaces, complete metric spaces.

Unit-5

Product Spaces: Arbitrary product spaces, product invariance of certain separation and countability axioms, Tychonoff's Theorem, product invariance of connectedness.

Outcomes: Upon successful completion of the program the students will be aware of:-

- The definitions of standard terms in topology.
- How to read and write proofs in topology with a variety of examples and counter examples.
- Some important concepts like continuity, compactness, connectedness, projection mapping etc
- Countability, separation axioms and convergence in topological spaces.
- Using new ideas in mathematics and also help them in communicating the subject with other subjects.

Text book:

- J.N. Sharma, Topology, Krishan Prakashan Media (P) Ltd. Meerut Delhi.
- J.M. Munkers, Topology, Publication Tata McGraw Hill.
- H.K.Pathak, Topology, Shisksha Sahitya Prakashan Meerut.

References Book:

- G.F. Simmons, Introduction to topology and modern analysis, Tata McGraw Hills.
- K.D. Joshi, Introduction to General Topology, Wiley Eastern.

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SEMESTER- 2nd **Subject Code: 4010211404**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: COMPLEX ANALYSIS-II **Theory Min. Marks: 28**

Objectives:

- To introduce the concept of zero is and singularities of a complex valued function.
- To introduce residues theorem as well as some definite integral round the unit circle.
- To introduce the concept of integral of rational function on the semi circular region.
- To introduce the concept of fixed point and bilinear transformation and their special from.
- To introduce the concept of analytic function and multiple valued function.

Unit-1

Fundamental theorem of integral calculus for complex functions, uniqueness theorem, The zero of an analytic function, Singularities of an analytic function.

Unit-2

Residues, Cauchy's residue theorem, Evaluation of real definite integrals by contour integration, Integration round the unit circle.

Unit-3

Evaluation of the integral . Evaluation of the integrals of the form , , m>0, where P(x),Q(x) are polynomials,deg Q(x) > deg P(x) Q(x)=0 has no real roots.

Unit-4

Fixed points or Invariant points of a Bilinear transformation, Normal form of a Bilinear transformation, Elliptic, Hyperbolic and parabolic transformations, some special Bilinear transformations.

Unit-5

Analytic, Holomorphic and Regular function, Polar form of Cauchy-Riemann Equations, Derivative of w = f(z) in polar form, orthogonal System, Multiple Valued function.

Outcomes:

- Understanding the concept of singularities will help student to find integral of complex valued function on some simple connected region and multi connected region.
- Students will able to solve definite integral easily which is quite difficult by analytical method.
- Understanding fixed point would help students to learn more about those type of function which posses fixed point.
- Students will learn more about everywhere differentiable function and they will learn how it helps them to decide analyticity of function.

Text book:

- Dr. H.K. Pathak, Complex Analysis, Shiksha Sahitya Prakashsn Meerut.
- J.N. Sharma, Complex Functions, Krishan Prakashan Media (P) Ltd. Meerut Delhi.

References Book:

- V.S. Tyagi, Functions of a complex variable, Kedarnath Ramanath Delhi.
- S. Ponnusony, Foundation of Complex analysis, Narosa Publishing House.
- John & Mathews Russell Wottowell, Complex analysis for Mathematics & Engineering.

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SEMESTER- 2nd **Subject Code: 4010211405**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: DIFFERENTIAL EQUATION-II **Theory Min. Marks: 28**

Objective

- This course helps the students to study Linear and Non linear differential equations.
- To introduce the concept of boundedness of solutions.
- Understanding the concept of Legendre polynomials.
- To understand the Legendre's function of the second kind.

Unit-1

Linear and Non-linear differential equation, Independence of constants of integration, some theorems on second order linear differential equations, Linear dependence and independence of solutions of an equations.

Unit-2

Boundedness of solutions, L^2- Boundedness, Oscillatory equations, Number of zeros, The adjoint equation, Lagrange's identity, Greens formula, Lagrange's identity in case of second order, Self-adjoing.

Unit-3

Legendre polynomials, Solution of Legendre's equation, Definition of $P_n(x)$ and $Q_n(x)$, Orthogonality, Recurrence formulae, Christoffel's summation formula.

Unit-4

Rodrigue's formula, Even and Odd functions, Expansion of x^n in Legendre's polynomials, General results.

Unit-5

Legendre's function of the second kind, Neumann's Integral, Recurrence formulae for $Q_n(x)$, Relation between $P_n(x)$ and $Q_n(x)$, Christoffel's second summation formula.

Outcomes:

- The student will be able to define the elementary concept of Linear and non linear differential equations.
- The student will be able to define and work with the concept of Boundedness of solutions and Langrange's identity.
- The student will be able to define and work with the concept of Legendre's polynomial.
- The student will be able to apply the Neumann's integral and Christoffel's summation formula.

Text book:

- Sharma-Gupta, Differential Equation, Krishan Prakashan Media (P) Ltd. Meerut Delhi.
- H.K Pathak and J. P. Chauhan, Differential Equation, Shiksha Sahitya Prakashan Meerut.

References Book:

- Ravi P.Agrawal and Ramesh C.Gupta, "Essentials of Ordinary Differential Equations" McGraw-Hill Book Company,1993.
- Elsgolts, "Differential equation and the calculus of variations", MIR publications,1980.

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SEMESTER- 3rd
Course: M.Sc. Mathematics
SUBJECT: Functional Analysis-I

Subject Code: 4010311401
Theory Max. Marks: 70
Theory Min. Marks: 28

Objectives:

- Understand the Normed linear spaces and Banach spaces.
- Be familiar with the sub space and Quotient space of Banach Space.
- Understand compactness, Equivalent norms Hahn Banach theorem.
- Understand the concept of Natural imbedding theorem and Riesz lemma.
- Get exposed to the conjugate space and the conjugate of an operator.

Unit -1

Normed linear space, Banach spaces examples and theorems, Holders inequality, Minkowski's inequality, Cauchy's inequality.

Unit -2

Completeness of C^n, the space l_p^n, the space l^p, the space l_∞^p, the space l_∞, The Classical Banach spaces L_p.

Unit -3

Sub space and Quotient spaces of Banach space , Norm of Bounded (continuous) linear transformation , basic properties of finite dimensional normed linear space.

Unit -4

Compactness , Equivalent norms , Riesz –lemma ,Convexity , Hahn Banach Theorem, Generalized Hahn Banach theorem .

Unit -5

The natural imbedding of N in N** , the conjugate space of l_p, the Open mapping theorem, Closed graph theorem , uniform boundedness theorem, the conjugate of an operator .

Outcomes:

- To learn to recognize the fundamental properties of normed linear space and to learn classify the standard examples.
- To understand the Banach space.
- Demonstrate accurate and efficient use of compactness.
- To explain the conjugate space and learn to use properly the specific techniques for conjugate of an operators over the Banach space.

Text book:

- J.N. Sharma A.R.Vashishtha, Functional Analysis, Krishna Prakashan Media (P) Ltd. Meerut Delhi.
- P.K.Jain & O.P. Ahuja & K. Ahamad, Functional Analysis, New Age International (P) Ltd. Wiley Eastern Ltd. New Delhi, 1997.
- K.K.Jha, Functional Analysis, Students Friends 1986.
- H.K.Pathak, Functional Analysis, Shiksha Sahitya Prakashan Meerut.

References Book:

- V.Choudhari & Sudarshan Nanda, Functional Analysis with applications, Wiley Eastern Ltd. New Delhi.
- D. Somsundaram, A First Course in Functional Analysis, Narosa Publishing House, New Delhi.

Dr. C.V. RAMAN UNIVERSITY

Kargi Road, Kota, Bilaspur (C.G.)

SEMESTER- 3rd **Subject Code: 4010311402**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: Integral Transform-I **Theory Min. Marks: 28**

Objectives:

- To expose students to learn Laplace and Fourier transform.
- To equip students with the methods of finding Laplace transform and Fourier transform of different functions.
- To make students familiar with the methods of solving IVP and BVP using laplace and fourier transform.
- To make students informative to complex fourier transform.

Unit –I

Definition and Properties, Sufficient Conditions for the existence of Laplace Transform, Laplace Transform of some elementary functions, Laplace Transform of the derivatives, Inverse of Laplace Transform, Initial and final theorems, Learch's theorem, Heaviside's expansion theorem, Convolution theorem.

Unit-II

Some of ordinary Differential Equations with Constant Coefficients, Solution of ordinary differential equation with variable coefficients, Solution of Simultaneous ordinary differential equation, Solution of Partial differential equations, Application to electrical equations, Application to mechanics, Application of Laplace transform to integral equations.

Unit-III

Application of Laplace transform in initial Boundary value problems, Heat conduction equation, Wave equation, Laplace equation Application to Beams.

Unit-IV

Dirichlet's condition, Fourier series, Fourier integral formula, Fourier transform or complex Fourier transform, Inversion theorem for complex Fourier transfor, Fourier Sine and Cosine Transform, Change of Scale Property, Shifting Property, Modulation theorem, Multiple Fourier transform, Convolution, The Convolution or Falting theorem for Fourier transform, Parseval's identity for Fourier transform.

Unit-V

Finite Fourier sine transform, Inversion formula for sine transform, Finite Fourier cosine transform, Inversion formula for cosine transform, Multiple finite Fourier transform theorems on operational properties of finite sine and cosine transform, Combined properties of finite Fourier sine and cosine transform.

Outcomes: Upon successful completion of this course, students will be able

- To calculate the Laplace transform and Inverse Laplace Transform of standard functions.
- To select and use the appropriate shift theorems in finding laplace and inverse laplace transform.
- To combine the necessary Laplace transform techniques to solve second order differential equations.
- To find the complex Fourier transform of some functions .
- To find the Fourier transform of some elementary and standard functions with properties of finite Fourier sine and cosine transform.

Text book:

- D.C. Agrawal, Advance Integral Transforms,
- Goel & Gupta, Integral Calculus,

References Book:

- I.N. Sneddon, The Uses & Integral Transform,
- C.J.Tranter, Integral Trnasform

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Kargi Road, Kota, Bilaspur (C.G.)

SEMESTER- 3rd **Subject Code: 4010311403**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: Partial Differential Equation **Theory Min. Marks: 28**

Objectives:

- Learn to solve Partial Differential Equation of Second Order.
- To make students familiar with Green's Function and Harmonic Function.
- Understand the application of Partial Differential Equations.
- Learn to solve fundamental solution of Laplace equation.

UNIT – 1 Partial Differential Equation of Second Order:
Introduction, Classification of Linear partial differential equations of second order, canonical forms, The solution of linear Hyperbolic equations, Riemann method of solution of general hyperbolic equation of the second order.

UNIT – 2 Green's Function and Harmonic Function:
Introduction, Green's function for Laplace equations, The method of images, The Eigen function method, Green's function for the Wave equation- Helmholtz theorem, Green's function for diffusion equation, Properties of harmonic functions, The spherical mean,Mean value theorem for Harmonic function.

UNIT – 3 Application of Partial Differential Equations:
Introduction, Practical problems involving PDE, One dimensional wave equation, Two dimensional wave equation, Heat equation, One and two dimensional Heat equation, Diffusion equation, Method of separation of variable or product method.

UNIT – 4
Solution of Laplace's equation in polar coordinates, Vibration of a circular membrance, Laplace's equation in terms of spherical coordinates, Laplace's equation in terms of sylindrical co-ordinates.

UNIT – 5
Fundamental solution of Laplace equation, Poisson's equation, Regularity, Local estimates for harmonic functions, Maximum-Minimum principle, Green's identities, Applications of Green's identities, Dirichlet condition, Representation formula, Harnack's inequalities, energy methods.

Outcomes: After completion the students will be able to:

- Solve Partial Differential Equation of Second Order.
- Solve some problems of Green's Function and Harmonic Function.
- Understand the application of Partial Differential Equations
- Find the solutions of Laplace equation and Poisson's equation.

Text Book:

- Singh & Chauhan ,Introduction of Partial Differential Equations, Shiksha Sahitya Prakashan ,Meerut.
- K. Shankar Rao, Introduction of Partial Differential Equations, Prentice Hall of India P.Ltd.New Delhi.

References book:

- I. N. Sneddon, F. John, P. Prasad and R. Ravindran, Amarnath, Partial Differential Equations.
- I. M. Gelfand and S. V. Fomin, Calculus of variations, Prentice Hall of India P.Ltd.New Delhi.

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SEMESTER- 3rd **Subject Code: 4010341402**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: Advanced Discrete Mathematics (Elective – I) **Theory Min. Marks: 28**

Objective:- The aim of the course is to develop students

- a solid understanding of algebraic structure and also the advanced concepts covered in the course.
- to use techniques from algebra, analysis and probability to solve problems in discrete mathematics.
- A solid understanding about semigroups, monoids, lattices and trees.
- a good grasp of the applications of this subject in other areas of mathematics and to real world problems.

UNIT – 1

Algebraic Structures : Introduction , Algebraic Systems : Examples and General Properties : Definition and Examples , Some Simple Algebraic Systems and General Properties , Homomorphism and Isomorphism congruence relation ,.

UNIT – 2

Semigroup & Monoids : Defination & Examples , Homomorphism of semigroups and Monoids

UNIT – 3

Lattices : Lattices as Partially ordered Sets : Defination and Examples , Principale of duality , some Properties of Lattices , Lattices as Algebraic Systems , Sublatttices , Direct Product and Homomorphism.

UNIT – 4

Some special Lattices e.g. complete , Complemented and Distributive Lattices , Boolean Algebra : definition and Examples , Subalgebra , Direct product and Homomorphism , Join irreducible , atoms and antiatoms.

UNIT – 5

Trees : Trees and its properties, minimally connected graphs pendant vertices in a tree, distance and centers in a tree , rooted and binary tree Levels in a binary tree , height of a tree , Spanning tress , rank and Nullity.

Outcome:- Upon successful completion of this course, the students will be able to:

- Understand the basic principles of sets and operations in sets.
- Demonstrate different traversal methods for trees and graphs.
- Write model problems in mathematical science using trees and graphs.
- Evaluate Boolean functions and simply expressions using the properties of Boolean algebra.

Text book:

- Swapan Kumar Sarkar, Discrete Mathematics , S. Chand & company Ltd. Ram Nagar ,New Delhi.
- H. K. Pathak, Advanced Discrete Mathematics ,Shiksha Sahitya Prakashan, Meerut.
- Udit Agrawal , Discrete mathematical Structure, Dhanpat Rai & Co.(P) Ltd, Delhi.
- M. K. Gupta, Discrete Mathematics, Krishna Prakashan Media (P) Ltd. , Meerut.

References Book:

- J.P. Tremblay & R. Manohar, Discrete Mathematical Structures with applications to Computer science, Mc-Graw Hill Book Company,1977.
- C.L. Liu, Elements of Discrete Mathematics, Mc-Graw Hill Book Company.
- S.Lepschutz, Finite Mathematics, Mc-Graw Hill Book Company.

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Kargi Road, Kota, Bilaspur (C.G.)

SEMESTER- 3rd **Subject Code: 4010341406**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: Numerical Analysis (Elective – I) **Theory Min. Marks: 28**

Objectives:

- This course aims to provide the information about systems of linear equations.
- This course helps to study the different methods of Interpolation, Differentiation and Integration.
- To understand the concept of approximation of functions.
- To introduce the concept of Ordinary and Partial differential equations.
- This course helps to gain skill in problem solving and critical thinking.

Unit-1 Systems of Linear equations and Algebraic Eigen value Problems

Direct Method: Gauss elimination method, Error analysis, **Iterative methods**: Gauss Jacobi and Gauss-Seidel method, Convergence considerations, Eigen value problem: Power method.

Unit-2 Interpolation Differentiation and Integration

Interpolation: Lagrange's and Newton's interpolation, Errors in interpolation, Optimal points for interpolation, Numerical differentiation by finite differences, **Numerical integration**: Trapezoidal, Simpson's and Gaussian quadratures, Error in quadratures.

Unit-3 Approximation of functions

Norms of functions, **Best approximations**: Least squres polynomial approximation, Approximation with Chebyshev polynomials, Piecewise linear and cubic spline approximation .

Unit-4 Ordinary Differential Equations

Single step methods: Euler's method, Taylor series method, Runge-Kutta method of fourth order, **Multistep methods**: Adam's Bashforth and Milne's Thomson method, Stability considerations, **Linear two point BVPs**: Finite difference method.

Unit-5 Partial Differential Equations

Elliptic Equations: Five point finite difference formula in rectangular region, Truncation error; **One dimensional parabolic equation**: Explicit and Crank – Nicholson schemes; Stability of the above schemes, **One dimensional hyperbolic equation:** explicit scheme.

Outcomes:

- The student will be able to solve the system of linear equations and algebraic eigen value problems.
- Understanding the ideas of solving interpolation, differentiation and integration.
- Fluency in solving approximation of functios.
- The student will be able to solve ordinary differential equation by various methods.
- The student will be able to solve elliptic,one dimensional parabola and hyperbola equations.

Text book:

- Brian Bradie, " A friendly introduction to numerical analysis", Pearson education, New Delhi, First edition,2007.
- Kincaid D. and Chenney W., "Numerical Analysis: Mathematics of scientific computing", Brooks/Coles Publication of second edition, 2002.

References Book:

- Isaacson E.and Keller H.B., " analysis of Numerical methods" Dover Publication,1994.
- Philips G.M. and Taylor P.J., " Theory and applications of numerical analysis",Elsevier, New Delhi,second edition 2006.
- Jain M.K.,Lyenger S.R.K. and Jain R.K., " Numerical methods for Scientific and Engineering", New age International Pub. Co., 3rd edition, 1993.
- Conte S.D. and Carl De Boor, "Elementary numerical analysis", Tata Mc Graw Hill Publishing Company, 3rd edition,2005.

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SEMESTER- 3rd **Subject Code: 4010341407**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: Mathematical Statistics (Elective – I) **Theory Min. Marks: 28**

Objectives:

- To tell sampling distributions and estimation theory.
- To introduce the concept of testing of hypothesis.
- To introduce the concept of correlation and regression.
- In particular to study the design of experiments.
- This course helps to study multivariate analysis.

Unit-1 Sampling Distributions and Estimation Theory

Sampling distributions, Characteristics of good estimators, Method of moments, Maximum likelihood estimation, Interval estimates for mean, Variance and Proportions.

Unit-2 Testing of Hypothesis

Type I and Type II errors, Tests based on normal, t, χ^2 and F distributions for testing of mean, variance and proportions, Tests for independence of attributes and goodness of fit.

Unit-3 Correlation and Regression

Method of least squares, Linear regression, Normal regression analysis, Normal correlation analysis, Partial and multiple correlation, Multiple linear regression.

Unit-4 Design of Experiments

Analysis of variance, One way and two way classifications, Completely randomized design, Randomized block design, Latin square design.

Unit-5 Multivariate Analysis

Covariance matrix, Correlation matrix, Normal density function, Principal components, Sample variation by principal components, Principal components by graphing.

Outcomes:

- The student will be able to solve the Mean, Variance and Proportions.
- The student will be able to find Type I and Type II errors by various distributions methods.
- The student will be able to apply method of least squares.
- The student will be able to study the analysis of variance.
- The student will be able to study covariance matrix, correlation matrix and principal components by graphing.

Text Book:

- J.E. Freund, "Mathematical Statistics", Prentice Hall of India, 5th Edition, 2001. (Chapters; 8,10,11,12,13,14,15)
- R.A. Johnson and D.W. Wichem, "Applied Multivariate Statistical Analysis", Pearson Education Asia, 5th Edition, 2002.

References Book:

- Gupta S.C. and Kapoor V.K., "Fundamentals of Mathematical Statistics", Sultan Chand and Sons, 11th Edition, 2003.

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SEMESTER- 3rd **Subject Code: 4010341408**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: Special Function (Elective – II) **Theory Min. Marks: 28**

- To study the Gamma function and related functions.
- To introduce Hypergeometric differential equations and generalized Hypergeometric differential equation.
- This course helps to solve Hermite's differential equation.
- To introduce the Laguerre Polynomials.
- To introduce the Jacobi Polynomials.

UNIT – 1 Gamma Function and Related Functions

Eulerian definition, Weierstrass defination, Euler's Product $\Gamma(z)$, Evaluation of $\Gamma'(1)$ and $\frac{\Gamma'(\frac{1}{2})}{\Gamma(\frac{1}{2})}$, Equivalence of Weierstrass and Euler's definitions, Beta Function, Factorial Function, Gauss multiplication related functions.

UNIT – 2 Hypergeometric Function

Hypergeometric Function , Integral Represention of F(a,b ; c,z), Relation of contiguity , Hypergeometric differential equation , Transformations of F(a,b ; c,z) Introduction of generalized Hypergeometric Functions , Differential Equation Satisfied by ${}_pF_q$, Kummer's theorem, Ramanujan's theorem.

UNIT – 3 Hermit Polynomials

Introduction of Hermit Polynomials, Solution of Hermite's differential equation , Generating Function of Hermites Polynomials, value of $H_n(x)$ and its derivative at $x = 0$, Rodrigues Formula for $H_n(x)$, Recurrence relations for $H_n(x)$, Integral representation of Hermit Polynomial, Orthogonal Properties of $H_n(x)$.

UNIT – 4 Laguerre Polynomials

Introduction of Laguerre Polynomials, Solution of Laguerres differential equation,Generating function of Laguerre Polynomilas, Rodrigues Formula, Laguerre Polynomilas for particular values of n and x, Differential equations of $L_n(x)$, Orthogonal Properties.

UNIT – 5 Jacobi Polynomials

Introduction of Jacobi Polynomials, Generating Functions, Rodrigues Formula, Orthogonal Properties, Recurrence Releation.

Outcomes:

- The student will be able to solve the Gamma function and related functions.
- The student will be able to solve the Hypergeometric Function.
- The student will be able to solve the Hermit Polynomials.
- The student will be able to solve the Laguerre Polynomials.
- The student will be able to study the Jacobi Polynomials .

Text book:

- J.N.Sharma, Special function, Pragati Prakashan Meerut.
- H.K. Pathak, Special Function, Shiksha Sahitya Prakashan Meerut.

References Book:

- P.K Jain & O.P. Ahuja & K.Ahamad, Special Function, New international (P) Ltd. Wiley Eastern Ltd. New Delhi
- E.C. Titchmarsh, The theory of functions, Oxford University Press London.

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SEMESTER- 3rd **Subject Code: 4010341409**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: Differential Geometry (Elective – II) **Theory Min. Marks: 28**

Objectives:

- To introduce the theory of space curves.
- To introduce the concept of surface in R^3.
- To introduce the concept of Envelopes.
- To introduce the concept of Asymptotic lines and the fundamental equations of surface theory.
- To introduce the concept of Geodesics theorem and mappings.

UNIT- 1: Theory of space curves, arc length, tangent and normal's, Curvature and torsion of curve given as the intersection of two surfaces, Involute and Evolute .

UNIT- 2: The first and second fundamental form of a surface, Weingarton equation, Orthogonal trajectories, Mensuier theorem, Gaussian curvature, Euler's theorem, Dupin's theorem, Rodrigue's theorem, Dupin's indicatrix.

UNIT- 3: Envelopes, Edge of regression, Ruled surface, Developable surface, Monge's theorem, Conjugate directions.

UNIT- 4: Asymptotic lines, The fundamental equations of surface theory, Gauss's formulae, Gauss characteristics equations, Mainardi Codazzi equations, Weingarton equations, Bonnet's theorem on parallel surface.

UNIT- 5: Geodesics, Clairaut's theorem, Gauss Bonnet theorem, Conformal mapping and Geodesic mappings, Tissot's theorem, Dini's theorem.

Outcomes:

- The student will be able to solve the theory of space curves.
- The student will be able to solve the fundamental form of surface.
- Fluency in solving Envelopes and regression.
- The student will be able to solve the fundamental equations of surface theory.
- The student will be able to apply Geodesics theorem .

Text Book:

- T .J. Willmore, An introduction to differential geometry, oxford University Press, New York,1959.
- L.P. Eiscnhart, An introduction to differential geometry, Princeton University Press,Priceton, New jersey,1940.

References Book:

- M. Spivak, A compressive introduction to differential geometry.
- T .J. Willmore, Riemannian geometry, oxford University Press, USA.
- B.Sinha, an Introduction to modern differential geometry, Kalyani Prakashan,New Delhi, 1982.

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SEMESTER- 3rd
Course: M.Sc. Mathematics
SUBJECT: Number Theory (Elective – II)

Subject Code: 4010341410
Theory Max. Marks: 70
Theory Min. Marks: 28

Objectives:

- To introduce the concept Binomial theorem.
- To introduce the concept of Congruences and Techniques of Numerical calculations.
- To introduce the concept of Publickey cryptography.
- In particular to study the Combinational number theory.
- This course helps to study Farey sequences and functions.

Unit-1 Divisibility

Introduction, Divisibility, Primes, The Binomial theorem.

Unit-2 Congruences

Congruences, Solutions of congruences, The Chinese remainder theorem, Techniques of numerical calculations.

Unit-3 Application of Congruence and Quadratic Reciprocity

Publickey cryptography, Prime power moduli, Prime modulus, Primitive roots and Power residues, Quadratic residues, The Gaussian reciprocity law.

Unit-4 Functions of Number Theory

Greatest integer function, Arithmetic functions, Mobius inversion formula, Recurrence functions, Combinational number theory.

Unit-5 Diophantine Equations and Farey fractions

The equations $ax + by = c$ Pythagorean triangle, Shortest example, Farey sequences, Rational approximations.

Outcomes:

- The student will be able to solve Divisibility.
- The student will be able to find solutions of congruences.
- The student will be able to apply method of Congruence and Quadratic Reciprocity.
- The student will be able to study the analysis of Functions of Number Theory.
- The student will be able to study Diophantine Equations and Farey fractions.

Text book:

- Niven I., Zuckerman H.S. and Montgomery H.L., An introduction to the theory of numbers, John Wiley and Son's, 5th edition, 2004.

References Book:

- Graham R.L., Knuth D.E. and Patachink O. "Concrete Mathematics", Pearson education Asia , 2nd edition, 2002.
- Bressoud D., Wagon S., " A course in computational number theory", Key college publishing, 2000.

Dr. C.V. RAMAN UNIVERSITY

Kargi Road, Kota, Bilaspur (C.G.)

SEMESTER- 4th
Course: M.Sc. Mathematics
SUBJECT: Functional Analysis-II

Subject Code: 4010411401
Theory Max. Marks: 70
Theory Min. Marks: 28

Objectives:

- Understand the Inner product space and Hilbert space.
- Understand the Orthogonality .
- Be familiar with the concept of Riesz representation theorem for continuous linear functional on Hilbert space .
- Get exposed to the adjoint, self adjoint, Normal and Unitary operators.
- Understand Finite dimensional Spectral theory.

Unit -1

Inner product spaces , Hilbert spaces , some properties of Hilbert spaces ,Schwarz inequality

Unit -2

Orthogal complements , projection theorem , Ortthonarmel sets , Bessel's inequality ,complete Orthonarmal set .

Unit -3

The conjugate space H* ,Riesz representation theorem for continuous linear functional on a Hilbert space .

Unit -4

The Adjoint of an Oprtator , self adjoint operator , Normal and Unitary operators.

Unit -5

Finite Dimensional Spectral Theory- Eigenvalues and Eigenvectors,Existence of Eigenvalues,Matrix of a Linear Transformation, The spectral theorem.

Outcomes:

- To understand Hilbert space and the fundamental properties of it.
- To learn the application of Bessel's and Schwarz inequality.
- To explain the conjugate space of Hilbert space.
- To learn to use properly the specific techniques for operators over Hilbert space.
- To learn to use finite dimensional spectral theory .

Text book:

- J.N. Sharma A.R.Vashishtha, Functional Analysis, Krishna Prakashan Media (P) Ltd. Meerut Delhi.
- P.K.Jain & O.P. Ahuja & K. Ahamad, Functional Analysis, New Age International (P) Ltd. Wiley Eastern Ltd. New Delhi, 1997.
- K.K.Jha, Functional Analysis, Students Friends 1986.
- H.K.Pathak, Functional Analysis, Shiksha Sahitya Prakashan Meerut.

References Book:

- V.Choudhari & Sudarshan Nanda, Functional Analysis with applications, Wiley Eastern Ltd. New Delhi.
- D. Somsundaram, A First Course in Functional Analysis, Narosa Publishing House, New Delhi

Dr. C.V. RAMAN UNIVERSITY

Kargi Road, Kota, Bilaspur (C.G.)

SEMESTER- 4th
Course: M.Sc. Mathematics
SUBJECT: Integral Transform-II

Subject Code: 4010411402
Theory Max. Marks: 70
Theory Min. Marks: 28

Objectives:

- To apply the Fourier transform method for solving IVP and BVP.
- To learn Hankel transform and its properties.
- To apply Hankel transform in IVP and BVP.
- To understand the basic concept of Mellin transform and its properties.

Unit-I

Application of Fourier transform in initial and boundary value problems: Application of infinite Fourier transform, Choice of infinite sine or cosine transforms, Applications of finite Fourier transform, Finite Fourier transform of partial derivatives.

Unit-II

Definition of Hankel transform, Inversion formula for the Hankel transforms, Some important results for Bessel functions, Linearity property, Hankel transform of the Derivatives of a Function.

Unit-III

Hankel transform of (d^2 f)/〖dx〗^2 +1/x df/dx-n^2/x^(2) f. Parseval's Theorem .Definition of finite Hankel transform. Another form ofHankel transform.Hankel transform ofdf/dx.

Unit-IV

Hankel transform ofof(d^2 f)/〖dx〗^2 +1/x df/dx,where p is the root of the equationJ_n (ap) =0.Applications of HankelTransform in initial and boundary value problems.

Unit-V

Definition of Mellin transforms. The Mellin Inversion theorem. Linearity property. Some elementary properties & Mellin transform.Mellin transform of derivatives. Mellin transform of integrals. Convolution (or falting).

Outcomes: Upon successful completion of course the students will be able :

- To find the Hankel transform of some functions
- To apply the Fourier transform methods for solving functions.
- To demonstrate accurate and efficient use of Hankel transform techniques.
- To understand the application of Hankel transform
- To get exposed how to use the properties of Mellin transform in solving various functions.

Text book:

- D.C.Agrawal, Advance Integral Transforms,
- Goel & Gupta, Integral Calculus,

References Book:

- I.N. Sneddon, The Uses & Integral Transform,
- C.J.Tranter, Integral Trnasform

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SEMESTER- 4th **Subject Code: 4010441411**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: Metric Spaces and Fixed Point Theory (Elective – III) **Theory Min. Marks: 28**

Objectives:

- To introduce the concept of metric contraction principles.
- To introduce hyperconvex spaces and normal structure in metric spaces.
- To introduce continuous mapping in Banach spaces.
- This course helps to provide the basic information of metric fixed point theory.
- To introduce the Banach space ultra powers.

Unit-1 Metric Contraction Priciples

Banach contraction Principle, Further extension of Banach's principle, Caristis, Ekeland principle, Equivalence of the Caristis, Ekeland principle, Set values contraction,Generalized contractions.

Unit-2 Hyperconvex spaces and Normal structures in metric spaces

Hyperconvexity, Properties of Hyperconvex spaces, a fixed point theorem, Approximate fixed poits. Normal structures in metric spaces: a Fixed point theorem, Structure of the fixed point set, Fixed point set structure, Separable case.

Unit-3 Continuous mapping in Banach spaces

Brouwer's theorem, Further comments on Brouwer's theorem, Schauder's theorem, Stability of Schauder's theorem, Banach algebra's: Stone Weierstrass theorem, Leray, Schauder degree, Condensing mappings, Continuous mappings in hyperconvex spaces.

Unit-4 Meric fixed point theory

Contraction mappings, Basic theorem for non expansive mapping, Structure of the fixed point set, Asymptotically regular mapping, Set valued m,appings.

Unit-5 Banach space ultra powers

Some fixed point theorem, Asymptotically non expansive mappings, the Dami closedness principle.

Outcomes:

- The student will be able to understand the concept of Banach contraction principle.
- Understanding the concept of hyperconvexity and normal structure in metric spaces.
- The student will be able to apply Brouwer's theorem and Schauder's theorem.
- The student will be able to apply the basic concepts contraction mappings.
- The student will be able to apply the Demi closedness principle.

Text book:

- Mohamed A., Khamsi and William A. Kirk, " An introduction of metric spaces and fixed point theory", John Wiley and Son's,2011.

References Book:

- Zeidler E., "Non linear functional analysis and its applications", Vol. I , Springer – Verlag New York, 1986.
- Deimling K., "Nonlinear Functional Analysis", Springer – Verlag, New York, 1985.
- Smart D.R.., " Fixed Point Theory" Cambridge University Press, 1974.
- Istratescu V.I., "Fixed point theory", D.Reidel Publishing Company,Boston, 1979.

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SEMESTER- 4th **Subject Code: 4010441412**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: Measure and Integration Theory (Elective – III) **Theory Min. Marks: 28**

Objectives:

- To gain understanding of the abstract Measure Theory and definition and main properties .
- To construct Lebesgue Measure on the real line and in n- dimensional Euclidean space.
- To explain the basic advanced directions of the theory.

Unit-1
Measure of set, Lebesgue outer measure (Caratheodory), measurable sets, Algebra of measurable set, Measures of locally compact, Regularity, Housdroff space .

Unit -2
Measure space, measurable space , Lebesgue measure ,algebras, monotone classes.

Unit-3
Borel sets and their measurability, Measureable functions, Algebras of measurable functions.

Unit-4
Continuous function functions, Simple function, The structure of measurable functions , Lusin theorem.Sequence of mesearable function, Convergence in measure,.

Unit-5
Riesz theorem, Lebesgues monotone convergence theorem. Riemann sums and Riemann integral, Improper Integrals. Monotonic functions, types of discontinuity, functions of bounded variation, Lebesgue integral.

Outcomes:

- Students acquired basic knowledge of measure and integration theory .
- Analyze measurable sets and Lebesgue measure.
- Describe the Borel sets and Measureable functions.
- The student will be able to describe the structure of measurable functions.
- The student will be able to apply Riesz theorem and Lebesgues monotone convergence theorem.

Text Book :

- H.K.Pathak ,Real analysis ,Shiksha Sahitya Prakashan ,Meerut.
- P.K.Jain and V.P. Gupta ,Lebesgue Measure and Integration ,New Age International (P) ltd.

References Book :

- H.L.Royden ,Real analysis ,Macillan publishing Co.Inc.New York ,4th Edition ,1993
- G.de Barra ,Measure Theory and Integration ,Wiley Eastern Limited ,1981.

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Kargi Road, Kota, Bilaspur (C.G.)

SEMESTER- 4th **Subject Code: 4010441413**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: Object Oriented Programming (Elective – III) **Theory Min. Marks: 28**

Objectives:

- This course aims to provide the information about functions and classes in C++ .
- This course helps to study the Inheritance and Polymorphism in C++.
- To understand the concept of Input/ Output in C++.
- To introduce the concept of Java fundamentals.
- To introduce the concept of Java programming.

Unit-1 Functions and Classes in C++

Procedure oriented programming, Characteristics of OOP, Function prototype, Default arguments, Inline functions, Function overloading, Template functions, Classes, This pointer, Constructors, Destructors, Friend functions, Template classes, New and Delete operators, Operator overloading, Static members, Nesting of classes.

Unit-2 Inheritance and Polymorphism in C++

Single inheritance, Multiple inheritance, Hierarchical inheritance, Hybrid inheritance, Abstract base class, Virtual functions, Dynamic binding, Polymorphism, Virtual base classes.

Unit-3 Input/ Output in C++

Input/ Output operations, Overloading the insertion and extraction operators, I/O stream classes, File input/ output, exception handling.

Unit-4 Java Fundamentals

Features of Java, Classes, Inheritance, Packages, Interfaces, Exception handling.

Unit-5 Java Programming

Threading, Input/ Output operations, Applates, Event handling AWT controls, Layout managers.

Outcomes:

- The student will be able to solve the various functions and classes in C++.
- Understanding the ideas of various Inheritance and Polymorphism.
- Fluency in Input/ Output operations in C++..
- The student will be able to understand different features of Java.
- The student will be able to use Java programming**.**

Text book:

- S.B. Lipmann, "The C++ Primer", Pearson Education, 2000.
- Herbert Schildt, "The Complete Reference Java 2", Tata McGraw Hill, 7th Edition, 2004.

References Book:

- Robert Lafore, "Object Oriented Programming in C++", Galgotia Publications, 1995.
- E. Balaguruswamy, "Object Oriented Programming in C++", 4th Edition, Tata McGraw Hill, 2007.
- Ivory Horton, "Beginning C++", Wrox Press Ltd, 1998.
- John Hubbard, "Programming with C++", Tata McGraw Hill, 2nd Edition, 2006.
- Bjarne Stroustrup, "The C++ Programming Language", Pearson Education, 2005.
- E. Balaguruswamy, "Programming with Java", Tata McGraw Hill, 3rd Edition, 2007.

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SEMESTER- 4th **Subject Code: 4010441405**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: Operations Research (Elective – IV) **Theory Min. Marks: 28**

Objective: The aim of this course is to introduce students :-

- To establish theories and algorithms to model and solve mathematical optimization problems that translate to real life decisions making problems.
- To get exposed to the concept of linear programming problems and algorithm of linear programming problems.
- With some key topics such as, goal programming, transportation and assignment problems, network analysis and dynamic programming that will enable students to analyze the real life problems to reach at optimality.

UNIT – 1

Operation research and its Scope , Necessity of Operation Research in Industry , Linear Programming – Simplex Method, theory of the Simplex Method , Duality and Sensitivity Analysis .

UNIT – 2

Algorithms for Linear Programming- Dual Simplex Method , Parametric Linear Programming , Upper – Bound Technique , Interior Point Algorithm, Linear Goal Programming.

UNIT – 3

Transportation and Assignment Problems.

UNIT – 4

Networks Analysis – Shortest Path Problem , Minimum Spanning Tree Problem , Maximum Flow Problem , Minimum cost Flow Problem , Network Simplex Method , Project Planning.

UNIT – 5

Dynamic Programming- Deterministic and Probabilistic Dynamic Programming.

Outcomes : On completion of this course students will be able to:-

- Define and formulate linear programming problems and appreciate their limitations
- Solve LPP using appropriate techniques and optimization solvers, interpret the results obtained and translate solutions into directives for s.
- Conduct and interpret post-optimal and sensitivity analysis and explain their primal-dual relationships.
- Develop mathematical skills to analyze and solve integer programming, parametric linear programming and network models arising from wide range of applications.
- find maximum (of profit or yield) or minimum (of loss or cost) in real world objective.

Text book:

- R.K. Gupta Operations Research, Krishna Public House
- A.P.Verma Operetions Research, S.K. Kataria & Sons.

References Book:

- P.K.Gupta & D.S.Hira, Operations Research S.Chand & Company Ltd.
- R.Panneerselvan, Operations Research
- P.M.Karak Linear Programming Problem of Operation Research New Central Book Agency.

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SEMESTER- 4th
Course: M.Sc. Mathematics
SUBJECT: Fuzzy Set Theory (Elective – IV)

Subject Code: 4010441414
Theory Max. Marks: 70
Theory Min. Marks: 28

Objectives:

- To introduce the basic types and concepts of fuzzy sets.
- To introduce different operations on fuzzy sets.
- To introduce the concept of fuzzy arithmetic.
- To introduce the concept of fuzzy relation.
- To introduce the concept of fuzzy relation equations.

UNIT – 1 Basics

Basic types and concepts of fuzzy sets, Additional properties of α-cuts, Representations of fuzzy sets, Extension principle for fuzzy sets.

UNIT – 2 Operations on Fuzzy Sets

Types of operations, Fuzzy complements, Fuzzy intersections; t-norms, Fuzzy unions; t-co-norms, Combinations of operations.

UNIT – 3 Fuzzy Arithmetic

Fuzzy numbers, Linguistic variables, Arithmetic operations on intervals, Arithmetic operations on fuzzy numbers.

UNIT – 4 Fuzzy Relations

Crisp and fuzzy relations, Binary fuzzy relations, Binary relations on a single set, Fuzzy equivalence relations, Fuzzy compatibility relations, Fuzzy ordering relations.

UNIT – 5 Fuzzy Relation Equations

Partition, Solution method, Fuzzy relation equations based on sup-i compositions and inf-w_i compositions.

Outcomes: On completion of this course students will be able to:-

- Understand the basic concept of Fuzzy sets.
- Apply the operations on Fuzzy Sets.
- Solve the Fuzzy arithmetic.
- Understand the Fuzzy relations and Fuzzy relation equations.

Text book:

- George J. Klir and Yuan B., "Fuzzy Sets and Fuzzy Logic, Theory and Applications", Prentice Hall of India Pvt. Ltd., 1997 (Sections 1.3, 1.4, 2.1, 2.2, 2.3, Sections 3.1 to 3.5, Sections 4.1 to 4.4 and Sections 5.1, 5.3 to 5.7 and Sections 6.2 to 6.5).
- Sudhir K. Pundir and Rimple Pundir, Fuzzy sets and their application, Pragati Prakashan, Meerut.

References Book:

- Dubois D. and Prate H., "Fuzzy Sets and Systems, Theory and Applications", Academic Press, 1980.
- Kaufmann A., "Introduction to The Theory of Fuzzy Subsets", Vol.1, Fundamental Theoretical Elements, Academic Press, 1975.

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SEMESTER- 4th **Subject Code: 4010441415**
Course: M.Sc. Mathematics **Theory Max. Marks: 70**
SUBJECT: Advanced Graph Theory (Elective – IV) **Theory Min. Marks: 28**

Objectives: The aim of the course is to develop students:

- A solid understanding of the perfect graph and other class of perfect graphs.
- To understand Ramsey theory.
- A solid understanding about Extremal graph.
- A solid understanding about Connectedness in diagraph.
- To learn properties of Tournaments.

UNIT – 1 Perfect Graphs

The perfect graph theorem, Chordal graphs, Other class of perfect graphs, Imperfect graphs, The strong perfect graph conjecture.

UNIT – 2 Ramsey Theory

Ramsey's theorem, Ramsey number, Graph Ramsey theory, Sperner's lemma and Bandwidth.

UNIT – 3 Extremal Graphs

Encodings of graphs, Branchings and gossip, List coloring and choosability, Partitions using Paths and Cycles.

UNIT – 4 Connectedness in Digraphs

Digraphs, Connected and disconnected graphs, Strong digraphs, Digraphs and matrices.

UNIT – 5 Tournaments

Properties of tournaments, Hamiltonian tournaments, Score sequences.

Outcomes: Upon successful completion of this course, the students will be able to:

- Apply the perfect graph theorem.
- Apply Ramsey theory.
- Encode the graphs.
- Understand the connected and disconnected graphs.
- Understand the Hamiltonian tournaments.

Text book:

- M. Bezhad, G. Chartrand, L. Lesneik Foster, "Graphs and Digraphs", Wadsworth International Groups, 1995
- Douglas B. Waste, "Introduction to Graph Theory", Prentice Hall of India, 2002.

References Book:

- Martin Charles Golumbic, "Algorithmic Graph Theory and Perfect Graphs", Academic Press, 1980.
- Bela Bollabas, "Extremal Graph Theory", Dover Publications, 2004.
- Jorgan Bang-Jensen and Gregory Gutin, "Digraphs-Theory, Algorithms and Applications", Springer and Verlag London, 2001.

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SEMESTER- 4th
Course: M.Sc. Mathematics
SUBJECT: Project Work

Subject Code: 4010431401
Theory Max. Marks: 100
Theory Min. Marks: 50